Optically Discriminating Carrier-Induced Quasiparticle Band Gap and Exciton Energy Renormalization in Monolayer MoS₂

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Optoelectronic excitations in monolayer MoS₂ manifest from a hierarchy of electrically tunable, Coulombic free-carrier and excitonic many-body phenomena. Investigating the fundamental interactions underpinning these phenomena-critical to both many-body physics exploration and device applicationspresents challenges, however, due to a complex balance of competing optoelectronic effects and interdependent properties. Here, optical detection of bound- and free-carrier photoexcitations is used to directly quantify carrier-induced changes of the quasiparticle band gap and exciton binding energies. The results explicitly disentangle the competing effects and highlight longstanding theoretical predictions of large carrier-induced band gap and exciton renormalization in two-dimensional semiconductors.

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Introduction.-Monolayer transition metal dichalcogenide (ML-TMDC) semiconductors are exquisite optoelectronic materials that synergize the effects of strong confinement [1-3], intense many-body interactions [4-6], and spin-coupled valley degrees of freedom [7] in a robust, atomically thin semiconductor with extended twodimensional crystalline order. In ML-TMDCs, electronic excitations are collective phenomena that are described by a quasiparticle band structure that condenses the excitations into particles with momentum and energy that reflect the underlying many-body physics and crystal structure [8,9]. The energetic separation between the quasiparticle valence and conduction bands, termed the "quasiparticle band gap" or simply the "band gap", governs the electronic properties in ML-TMDCs such as transport, formation of Ohmic contacts, and band alignment in heterostructures [10–14]. Meanwhile, photoexcitations, which are essential to optoelectronic functionality [15–19], create electron-hole pairs within the quasiparticle band structure, forming a rich manifold of bound exciton states. The lowest-energy exciton-a strong dipole transition in these materials-determines the "optical band gap" (i.e., the energetic threshold of optical absorption, sometimes termed the "excitonic band gap"), which is energetically smaller than the quasiparticle band gap because of the electron-hole binding energy [20-22]. Strong physical and dielectric confinement makes Coulombic interactions central to determining these quasiparticle and optical band gaps, and an incredibly compelling aspect of ML-TMDCs is the ease by which the strength of this interaction can be manipulated, providing an unprecedented tunability of the quasiparticle and exciton energies [23-27].

In this Letter, we experimentally disentangle and quantify the carrier-induced renormalization of both quasiparticle and optical band gaps in ML-MoS₂, providing a unified picture of these rich and complex effects in two-dimensional semiconductors. This quantification is enabled by the direct, all-optical identification of the carrier-density-dependent quasiparticle band gap using photoluminescence excitation (PLE) spectroscopy combined with steady state electrostatic gating to control the strength of the Coulombic interactions in the ML-MoS₂. Importantly, renormalization effects on the quasiparticle band gap and exciton binding energy tend to counteract each other, leading to only minimal changes in the optical band gap [28]. Thus, in conventional optical absorption spectroscopy, without direct identification of the quasiparticle band gap, quasiparticle and excitonic renormalization effects must be inferred from higher-lying excitonic states [25,27,29,30]. Central to our approach, we demonstrate that the relative photoluminescence from defect-bound excitons (DXs) [31-33] diminishes with increased carrier doping and can identify the onset of photoexcitation of free carriers at the quasiparticle band gap. When combined with ground-state absorption and PLE spectroscopy, we can (1) track carrier-induced renormalization of the quasiparticle band gap and (2) fully deconvolve excitonic and quasiparticle renormalization effects. For both effects, we find



FIG. 1. (a) Schematic of gate-dependent PLE spectroscopy on monolayer MoS_2 . (b) Normalized PL spectra measured under different gate voltages with 2.5 eV excitation. The inset shows the dependence of defect PL yield as a function of gate voltage.

renormalization of more than 150 meV over a moderate range of doping concentrations, agreeing remarkably well with previous theoretical predictions [23] and providing the first explicit experimental discrimination of the carrierinduced renormalization of the quasiparticle band gap from that of the exciton states in a quantum many-body system. Further, we observe that at low doping levels the band gap and exciton binding energy can be larger than 2.7 eV and 800 meV, respectively.

Results and discussion.—Figure 1(a) shows a schematic of the PLE spectroscopy of back-gated ML-MoS₂ that reports the excitation-dependent photoluminescence as a function of free-carrier density (MoS2 grown on 285 nm SiO₂ on Si [34]). Complete experimental details are provided in Supplemental Material [35], but we note that all measurements were performed at 80 K where radiative recombination from the DX states is activated [31]. At unbiased gating, ML-MoS₂ flakes were found to be heavily n doped with a residual carrier concentration of 8.7×10^{12} cm⁻², which likely results from interactions with the underlying substrate [29,40]. Figure 1(b) shows the gate dependence of the relative intensities of the ground-state excitonic emission at $\sim 1.86 \text{ eV}$ (A exciton) and of the DX states at ~ 1.72 eV. When unbiased (e.g., $V_q = 0$ V), the PL of our samples is dominated by the trion [35]. Upon reducing the free carriers with increasingly negative gate voltages, the lower-energy emission from the DXs emerges: decreasing the concentration of free carriers increases the relative PL yield of the DX states with respect to the A excitonic emission. Previous work has indicated that DX emission is due to excitons Coulombically bound to charged sulfur vacancy sites [31-33]. Here, we show that the relative balance of DX and A exciton emission depends upon carrier concentration, suggesting that this Coulomb interaction is subject to carrier screening. A similar trend was also noted in ML-WS₂ [25]. To quantify this effect, we estimate the relative yield of the DX emission by calculating the ratio of emission below 1.80 eV to the total emission. And as evidenced in Fig. 1(b) (inset), which plots the ratio as a function of gate voltage, this



FIG. 2. Identification of the quasiparticle band gap in monolayer MoS_2 from PLE spectroscopy. (a) Dependence of the yield of DX emission on excitation energy (blue dots), overlaid on the absorption spectrum (gray, taken from samples transferred to a quartz substrate). The inset shows the color contour of normalized PL spectra measured at different excitation energies. (b) Comparison of the defect PL spectra (normalized to the *A* excitor; full spectra are shown in Supplemental Material [35]) under excitation energies that are on and off resonance of the continuum edge and *B* exciton. (c) Schematic level diagrams showing the relevant relaxation pathways of photogenerated excitations. A complete diagram is shown in Supplemental Material [35]. (d) Experimental PLE spectrum (gray dots) and total fit (black solid line) with contribution from the continuum (blue dotted line, with offset) and tail of the *C* exciton (magenta dotted line).

experimental observable can be used to detect changes in the free-carrier concentration in the system.

Figure 2 shows PLE spectroscopy of ML-MoS₂ at an intermediate carrier concentration, where emission intensities from the DXs and main *A* exciton states are comparable. In Fig. 2(a), the relative PL yield of the DX as a function of excitation energy is overlaid with the absorption spectrum in which the three prominent excitonic *A*, *B*, and *C* absorption resonances are identified [1,41]. First, the ratio of the DX emission to the *A* exciton emission generally increases with increasing excitation energy nearly in unison with the absorption from the higher-energy *C* band [41,42]. Secondly, a pronounced dip is observed at

2.07 eV, which corresponds to the resonance energy of the B exciton state. And finally, at 2.64 eV a small but pronounced decrease, deviating from the otherwise monotonic increase, is observed. Four individual PL spectra at representative energies are shown in Fig. 2(b), which exemplify the differences in the relative yield of DX emission.

The level diagram in Fig. 2(c) summarizes the absorption resonances and coupling pathways at these excitation energies in ML-MoS $_2$ [29,41]. Although the C exciton is peaked at ~2.9 eV, its absorption resonance is broad, yielding a tail of closely spaced excited states that spans nearly to the optical band gap. The narrower resonant excitations of the A and B excitons are superimposed on the C exciton at ~1.9 and ~2.1 eV, respectively. At each excitation energy, a fraction of the C excitons can relax to form A excitons [29,41] and DX states. The generally increasing trend of the DX emission yield vs excitation energy indicates that the relative coupling of C excitons to DXs strengthens with increasing energy. Direct excitation of B excitons, on the other hand, enhances the *relative* number of A excitons, presumably because this additional set of absorbing states lies in the same region of the Brillouin zone and preferentially couples to the A exciton, decreasing the relative DX yield at 2.07 eV.

For the higher-energy decrease in the DX yield at 2.635 eV, which is weaker than its lower-energy counterpart at ~ 2.07 eV, neither a strong excitonic resonance exists [29,30,43,44] nor are there any corresponding features in the absorption spectrum. Yet the PLE spectrum [Fig. 2(d)] of the total emission intensity exhibits a steplike increase at the same energy, which is well described as the sum of a broad increasing background (from the C exciton tail) and a broadened step function (see Supplemental Material [35] for details), similar to a feature observed in our previous work [29]. Such a steplike increase in photoexcitation is anticipated for the absorption at the band edge of noninteracting electrons in two dimensions [8,43,44]. In conjunction with the decrease in the DX yield, we reason that this energy marks the onset of photoexcitation of the continuum of unbound electrons and holes [44,45] near the quasiparticle band gap at the K/K' valleys. These unbound carriers reduce the emission yield of the DX states following the same mechanism as observed under electrostatic gating [Fig. 1(b)]. The approximate reduction of defect PL yield at 2.64 eV is 2%. Using the linear trend fitted from Fig. 1(b), such a reduction corresponds to an injected carrier concentration of 3×10^{11} cm⁻², which is of the same order as the estimated number of photoexcitations produced at these energies, of $\sim 8 \times 10^{10}$ cm⁻² (Supplemental Material [35]).

If our assertion is correct, the spectral signatures of direct excitation of the quasiparticle continuum in the PLE and relative DX yield should energetically shift with gate voltage as the quasiparticle band gap renormalizes [23].



FIG. 3. Gate-dependent PLE spectroscopy of monolayer MoS₂. (a) PLE spectra of the integrated emission measured at different gate voltages. Experimental data, total fit, and the continuum contribution (with offset) are represented as gray dots, blue solid lines, and blue dashed lines, respectively. The PLE intensities are normalized to the oscillator strength (i.e., step height) of the fitted continuum function. (b) The excitation-energy dependent relative yield of DX emission at different gate voltages. The arrows in (a) and (b) represent the same energy of E_{con} fitted from (a) as described in the text.

Gate-dependent PLE and DX emission yield spectra are shown in Fig. 3. At each gate voltage, the step feature in the PLE spectrum [Fig. 3(a)] and corresponding reduction in the relative yield of the DX emission [Fig. 3(b)] are observed (complete PLE data sets are shown in Supplemental Material [35]). Using the PLE spectra alone, the energetic threshold for optical excitation of the continuum of unbound quasiparticles (i.e., the continuum, E_{con}) is extracted from the position of a fitted step function (as described in Fig. 2) and is marked by the arrows in both the PLE and the relative DX emission yield spectra. Clearly, the two spectral features exhibit nearly identical renormalization effects. Starting at the residual doping concentration, $E_{\rm con}$ first shifts to lower energies as the gate voltage decreases to -40 V and then reverses directions, shifting to higher energies as gate voltage further decreases to -90 V, which was our lowest obtainable gate voltage before dielectric breakdown. For positive gate voltages, the continuum excitation features rapidly diminish



FIG. 4. Carrier-induced renormalization of the quasiparticle band gap of monolayer MoS_2 . (a) Dependence on electron doping concentration n_e of the measured continuum onset energy E_{con} (red squares) and quasiparticle band gap E_g (blue dots). Predicted quasiparticle band gap energies from previous studies [23,42, 47–49] are also plotted for comparison (orange crosses). (b) Direct comparison of the measured change of quasiparticle band gap (blue dots) to previous theoretical predictions (orange crosses) [23].

and are no longer clearly discernible possibly due to increased broadening of the continuum feature [45] and/or increased indirect optical absorption at higher carrier densities [46]. The strongly correlated renormalization of the step feature in the PLE and the reduction in DX emission yield offer compelling evidence that these spectral features are indeed related to the quasiparticle band gap, and that their spectral shifts with gate voltage provide important insight into carrier-induced renormalization effects.

Notably, direct band-edge and excitonic transitions are expected to behave markedly differently in response to changes in carrier density [28,45]. For example, the exciton absorption resonances renormalize by only $\sim 10 \text{ meV}$ [5], whereas the band gap energy is predicted to change by hundreds of meV [9] within a similar range of carrier concentration. To our knowledge, there are no excitonic states that are known nor predicted to renormalize over such a large energy range. In Fig. 4, the renormalization of the quasiparticle band gap is quantified and compared to previous theoretical studies. The dependence of the continuum onset energy, E_{con} , on carrier concentration is summarized in Fig. 4(a) where the gate voltage has been converted to the electron concentration, n_e (see Supplemental Material [35]). Careful distinction must now be drawn between the energetic onset of continuum excitations (E_{con}) and the quasiparticle band gap (E_a) . In a doped system, E_{con} is larger than E_q due to Pauli blocking, as direct transitions can only occur from occupied states in the valence band to unoccupied states in the conduction band above the Fermi energy, E_F [Fig. 4(a), inset]. Using a parabolic approximation for the band extrema, E_q is related to $E_{\rm con}$ by $E_g = E_{\rm con} - n_e \pi \hbar^2 / 2\mu q$, where \hbar is the reduced Planck constant, q is the electron charge, and μ is the exciton reduced mass [4]. From effective masses reported in the literature [42], the quasiparticle band gap (E_q) at the residual doping level ($n_e = 8.7 \times 10^{12} \text{ cm}^{-2}$) is calculated to be 2.57 ± 0.01 eV where the uncertainty reflects the variations of multiple measurements. With decreasing electron concentration, the measured quasiparticle band gap increases nonlinearly, reaching $2.70\pm0.01~\text{eV}$ at the lowest carrier concentration ($n_e = 1.8 \times 10^{12} \text{ cm}^{-2}$, $V_q = -90 \text{ V}$) achieved in our measurements. By fitting a line to quasiparticle band gap E_q at the four lowest electron concentrations, we estimate that E_q of our samples at intrinsic doping concentrations is 2.78 ± 0.02 eV. Remarkably, the majority of the theoretical predictions of quasiparticle band gap from previous studies [Fig. 4(a), orange crosses] [23,42,47–49] are within 100 meV of our estimated value. We also note that the band gap we measured at the residual doping condition is comparable to recent photocurrent [50] and PLE [29,30] measurements, but substantially higher than scanning tunneling microscopy (STM) measurements of ML-MoS₂ on conductive substrates [22,51]. And further, a recent STM study of suspended ML-MoS₂ [52] finds a gap approaching the value we determined for the zero-doping condition.

Such a large, nonlinear renormalization of the quasiparticle band gap has previously been theoretically predicted and attributed to carrier-induced screening [23]. In Fig. 4(b), our experimental measurement of the quasiparticle band gap renormalization is compared to theoretical predictions [23] where ΔE_g denotes the change of the band gap from the residual doping concentration. We find that for the relative changes in the quasiparticle band gap, the experimental and theoretical results agree remarkably well. Moreover, the observed band gap renormalization of over 150 meV is more than 1 order of magnitude larger than any excitonic renormalization effects in ML-TMDCs [4,25–27], further corroborating our assignment of the observed step feature in PLE spectra to the continuum.

Finally, in Fig. 5, the renormalization of the exciton binding energy is directly quantified by combining the PLE-derived values of the quasiparticle band gap and the optical band gap measured with gate-dependent absorption and PL spectra (Supplemental Material [35]). The extracted energies of the neutral A exciton (A^0) and charged A trion (A^{-}) states from absorption spectra are shown in Fig. 5(a). The corresponding carrier-dependent binding energy of A^0 can be calculated from its energetic separation from the quasiparticle band gap [Fig. 5(b)] and is found to be as large as 790 ± 17 meV at our lowest electron concentration. Extrapolating to lower concentrations, we estimate that the exciton binding energy at the zero-doping condition is 866 ± 31 meV, which is comparable to predictions by GW-Bethe-Salpeter equation calculations [42,48]. As the electron concentration is increased, the exciton binding energy rapidly decreases to 690 ± 15 meV at an electron concentration of $\sim 4.0 \times 10^{12}$ cm⁻² and then more gradually decreases to 660 ± 12 meV at the residual doping condition. This nonlinear behavior likely arises from the combined effects of increased Coulombic screening and phase space filling [53]. The resemblance between the renormalization trends for the quasiparticle band gap



FIG. 5. Carrier-induced renormalization of the exciton binding energy in monolayer MoS_2 . (a) Dependence of the absorption energies of the neutral *A* exciton (blue dots) and charged A^- trion (red diamonds) on gate voltage. (b) Renormalization of the binding energy of the neutral *A* exciton with electron concentration.

[Fig. 4(a)] and binding energy [Fig. 5(b)] reveals a linear relationship between these two (Fig. S9), similar to recent theoretical calculations predicting a general linear scaling law between exciton binding energy and quasiparticle band gap in two-dimensional materials [54,55]. We also note that carrier-induced effects on the quasiparticle band gap and binding energy counteract each other, resulting in comparatively modest changes in excitonic transitions.

In conclusion, using the suppression of defect emission by free carriers in combination with PLE, PL, and absorption spectroscopies, we have directly quantified carrierinduced quasiparticle and excitonic renormalization effects in gated ML-MoS₂ devices. At the lowest achieved doping level, the quasiparticle band gap is determined to be 2.70 ± 0.01 eV leading to an A exciton binding energy of 790 ± 17 meV. Both the quasiparticle band gap and binding energy renormalize by nonlinearly decreasing by over 150 meV as the electron concentration is increased to the residual doping level. Notably, our experimental results agree very well with previous theoretical predictions of the quasiparticle band gap [42,47,48] and renormalization effects [23]. As such, this spectroscopic approach serves as a facile way to identify the quasiparticle band gap in monolayer TMDC semiconductors in a broad range of device configurations, providing an all-optical compliment to STM [20,22,51,52,56]. For example, such information can be used in conjunction with ultrafast terahertz spectroscopy to study the rich many-body physics that govern exciton formation and coherence dynamics under both resonant and nonresonant excitation conditions [57-59]. Directly quantifying the fundamental quasiparticle band gap and exciton binding energies and their corresponding renormalization effects is essential for developing excitonbased optoelectronic devices in monolayer TMDC semiconductors that capitalize on their remarkable ability to tune the underlying many-body interactions.

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